



*Photo: R. Ketler, UBC*

## 10 Soil thermal properties



# Learning objectives

- Provide examples of why processes in the ground are of interest to climatologists.
- Know what are the key properties that describe the thermal behaviour of the soil / substrate in the climate system.
- Explain how the key properties relate to the process of heat conduction in soils.



# **Why might climatologists be interested in studying soil thermal properties and subsurface processes?**







Permafrost thawing on Ellesmere Island / Photo: A. Cassidy, UBC Geography





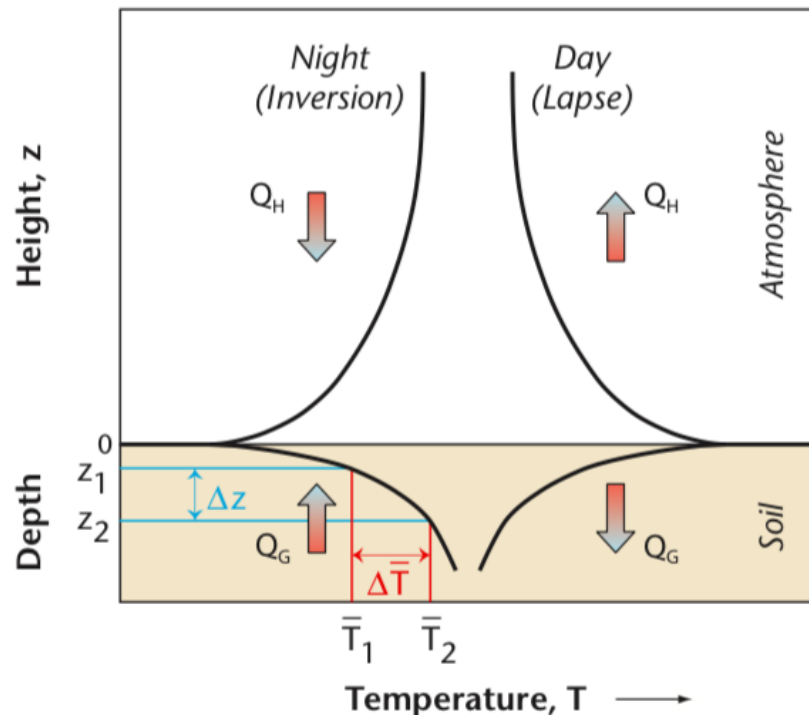




*Tonzi Ranch, California. Photo: J. Verfaillie*



# The role of the soil in the climate system



The influence of the **active surface** extends down into a relatively shallow layer of the substrate.

Nevertheless the properties of the shallow substrate layer make it a **significant volume of storage  $\Delta Q_s$**  of sensible heat and water over diurnal and annual scales.

Soils act as 'batteries' of energy forms and mass relevant in the atmosphere.



## Heat capacity and specific heat

---

Heat capacity  $C$  is the quantity of heat required to raise the temperature of a **unit volume** of a material through 1 K.



$\text{J K}^{-1} \text{m}^{-3}$

Specific heat  $c$  is the quantity of heat required to raise the temperature of a **unit mass** of a material through 1 K.



$\text{J K}^{-1} \text{kg}^{-1}$



# Heat capacity and specific heat of soil materials

Material	Heat capacity $C$ (MJ m <sup>-3</sup> K <sup>-1</sup> )	Specific heat $c$ (kJ kg <sup>-1</sup> K <sup>-1</sup> )	Density $\rho$ (Mg m <sup>-3</sup> )
Air	0.0012	1.01	0.0012
Water (liquid)	4.18	4.18	1
Ice	1.9	2.1	0.9
Soil mineral	2.1	0.8	2.65
Soil organic matter	2.5	1.9	1.3
Rock	2	0.8	2.7



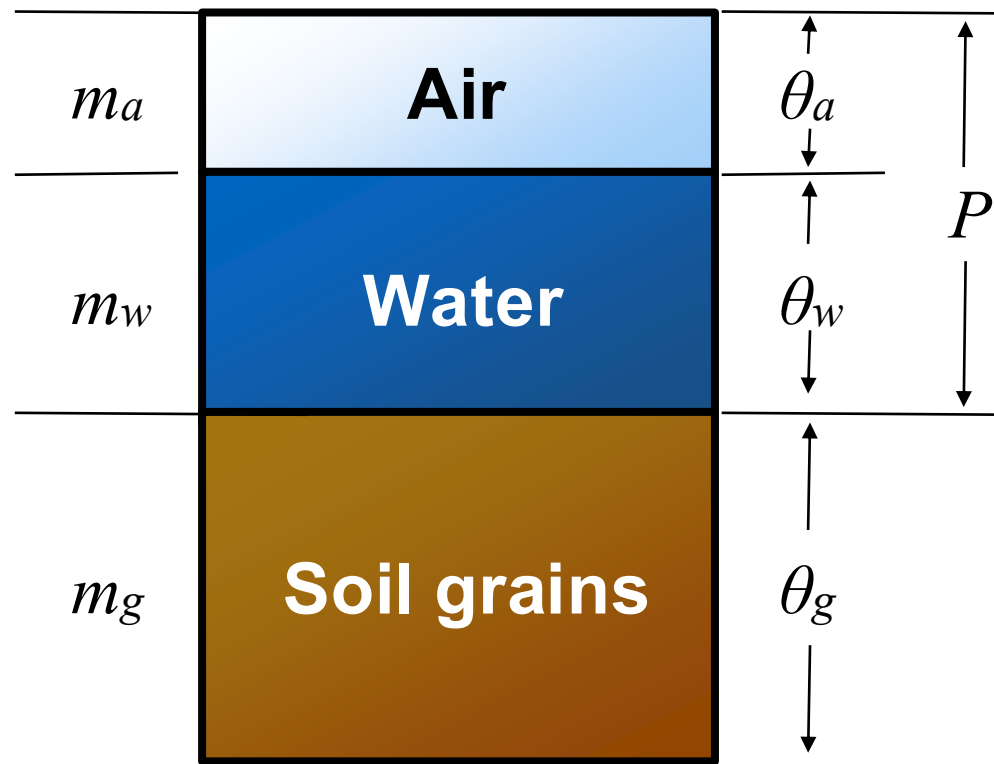
# Porosity, volume fractions and mass

## Mass

Expressed in mass  
(kg) of a sample

$$m_a + m_w + m_g = m_s$$

$m_s$  = total mass of soil



## Volume

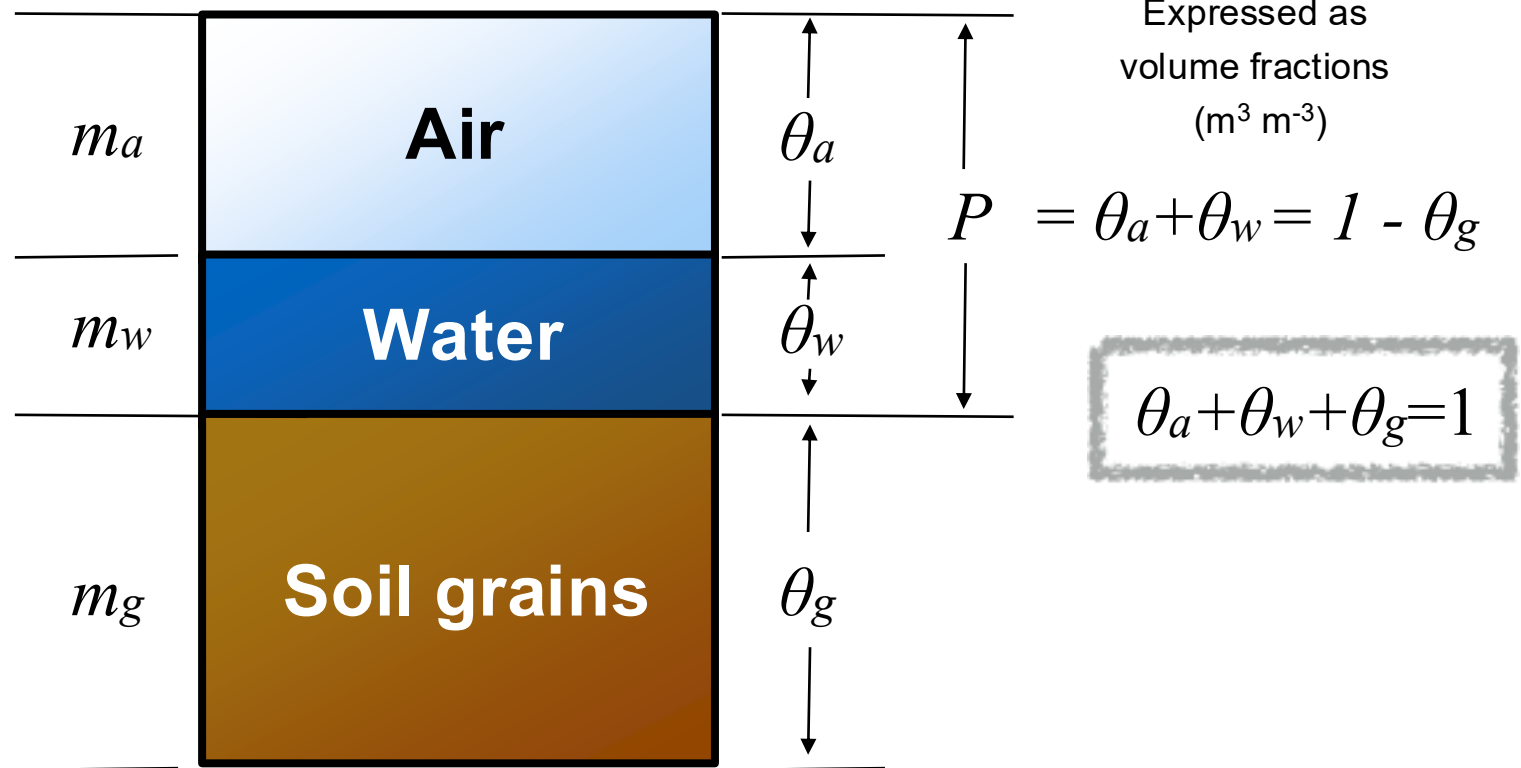
Expressed as  
volume fractions  
( $\text{m}^3 \text{ m}^{-3}$ )

$$P = \theta_a + \theta_w = 1 - \theta_g$$

$$\theta_a + \theta_w + \theta_g = 1$$

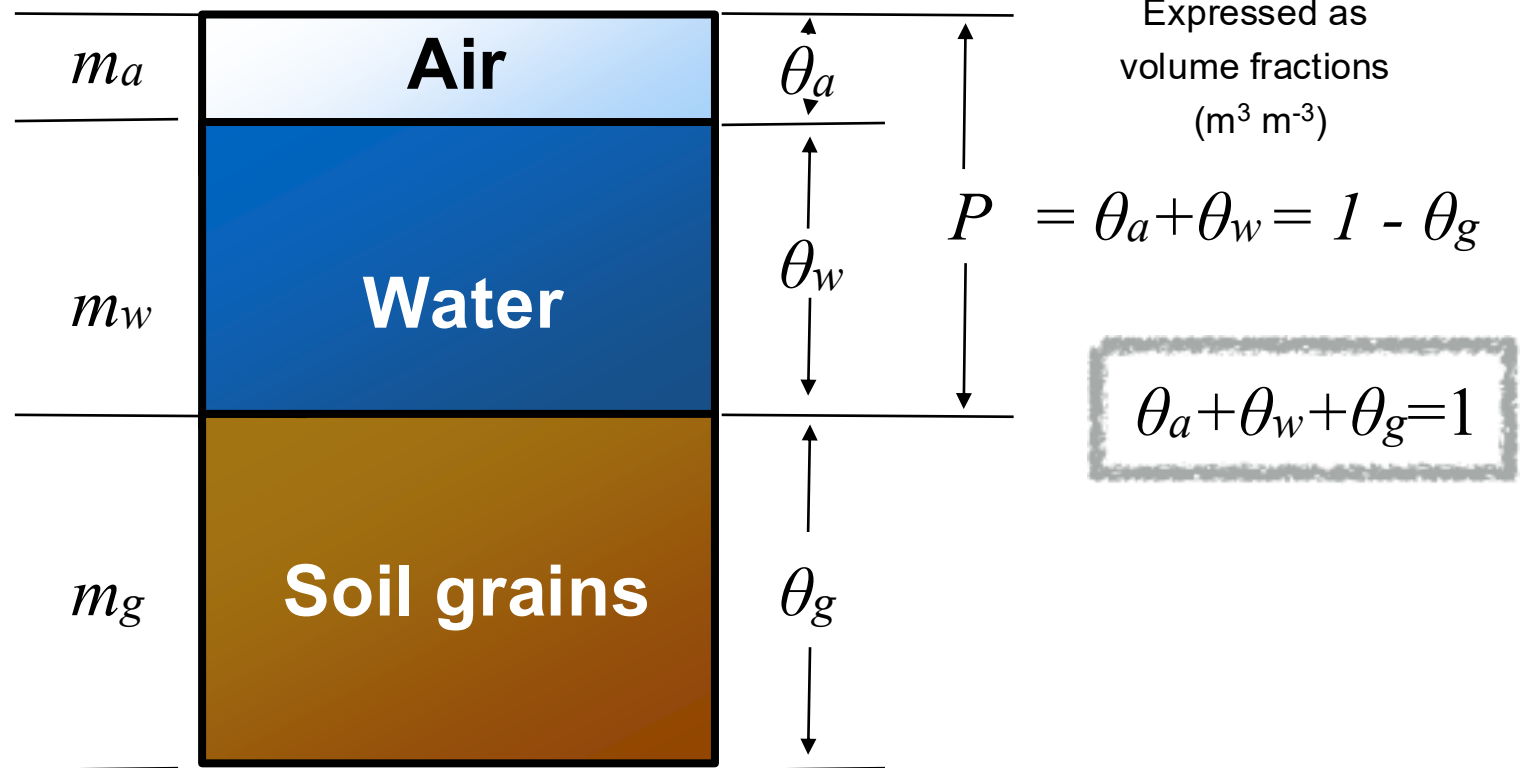


# Porosity, volume fractions and mass





# Porosity, volume fractions and mass





## Heat capacity of compound substances

---

The **heat capacity of a mixture** of substances such as soil can be calculated if the heat capacity and volume fraction of each component are known. In the case of soil,  $C_s$  is calculated using:

$$C_s = C_m \theta_m + C_o \theta_o + C_w \theta_w + C_a \theta_a \quad \star$$

where  $\theta$  is the volume fraction occupied by mineral (m), organic matter (o), water (w) and air (a).

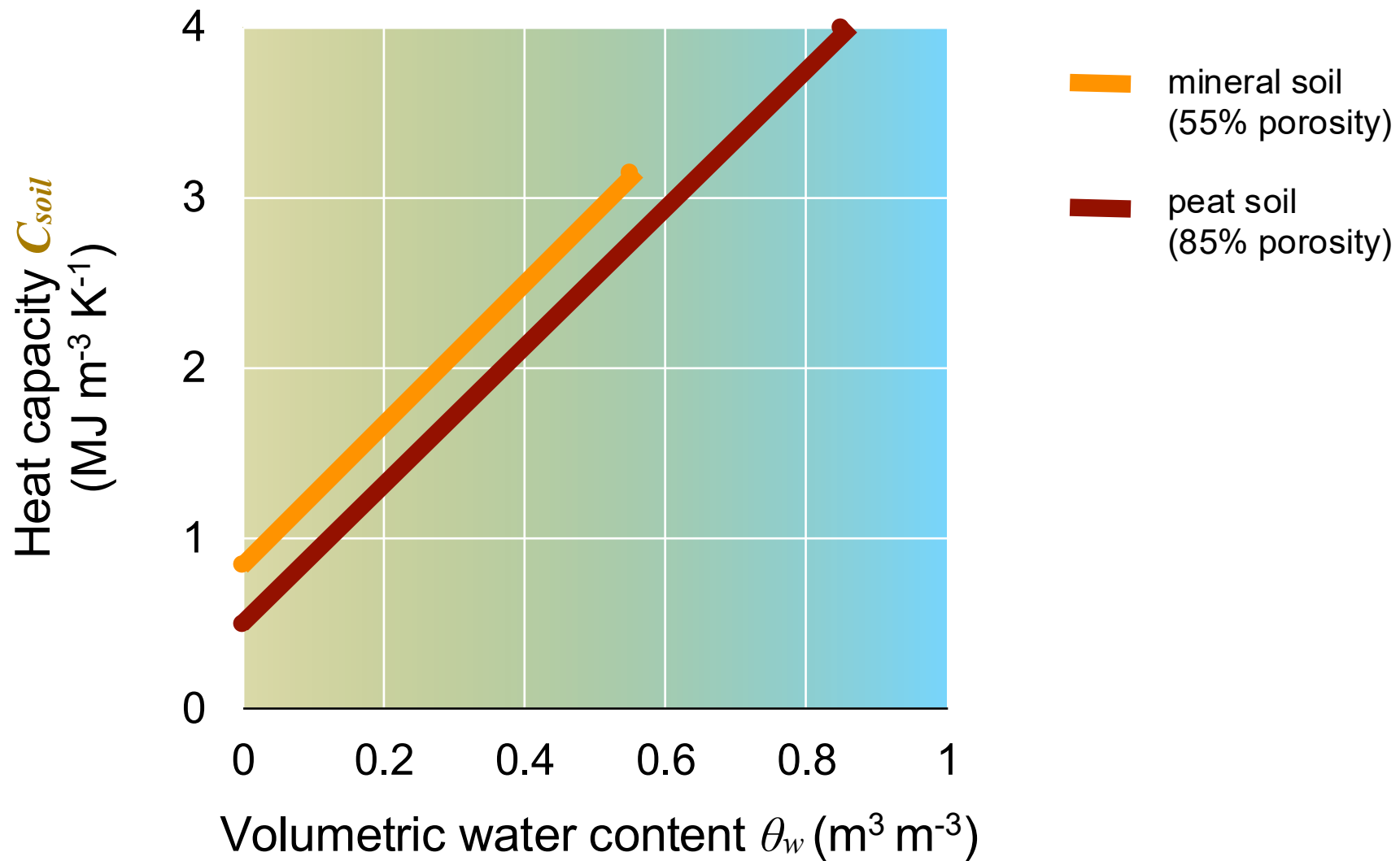
$C_a$  is very small relative to the other values of  $C$ , so it can be neglected.



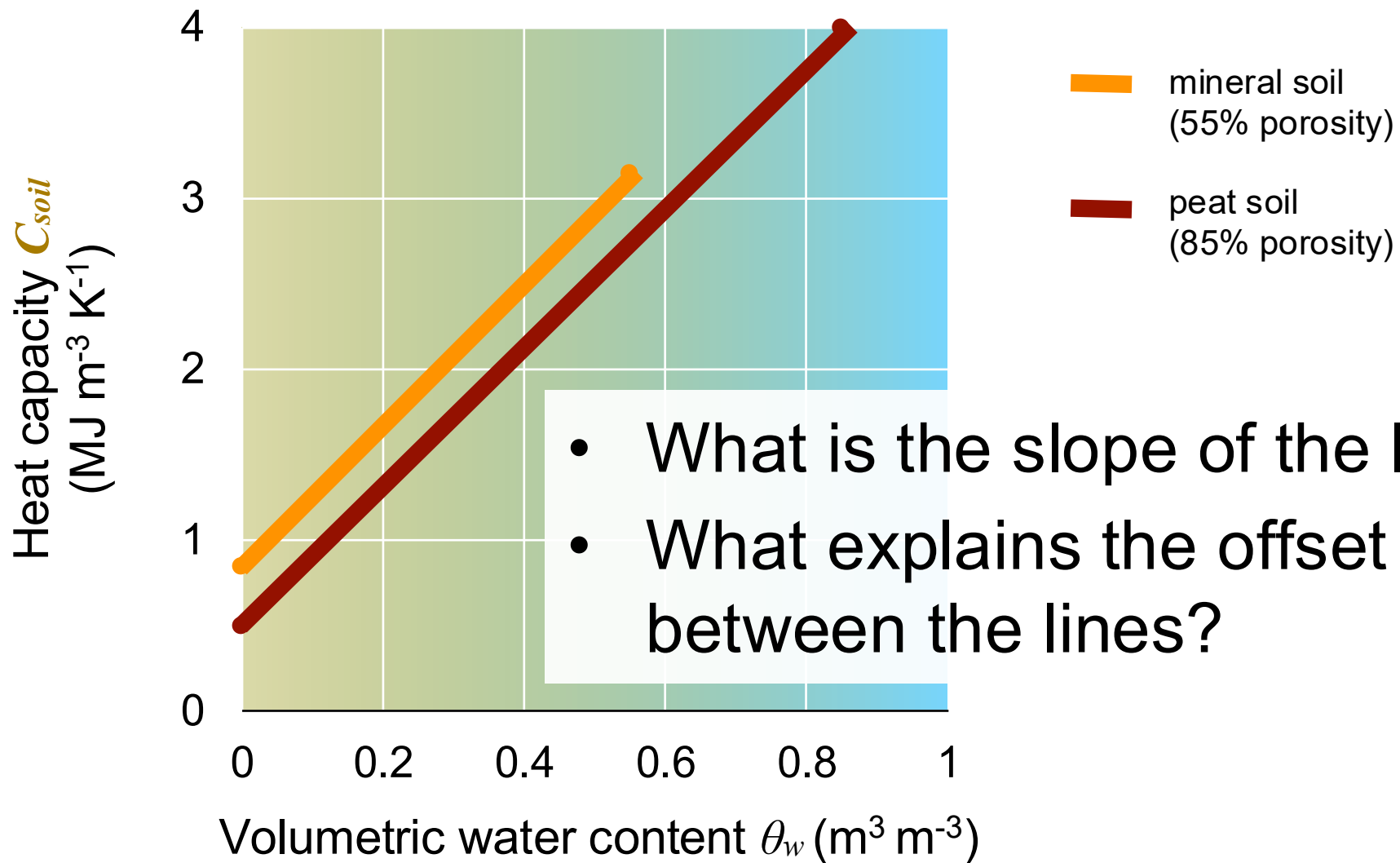




# Heat capacity and soil water content



## Heat capacity and soil water content





## Warming / cooling of a soil

---

Relating the **change of soil heat flux with depth** (the divergence of  $Q_G$ , i.e.  $\partial Q_G / \partial z$ ) to the **rate of temperature change** ( $\partial T / \partial t$ ) due to the **heat capacity** of the layer:

$$\frac{\partial Q_G}{\partial z} = C_s \frac{\partial T}{\partial t} \quad (\text{Eq 1})$$

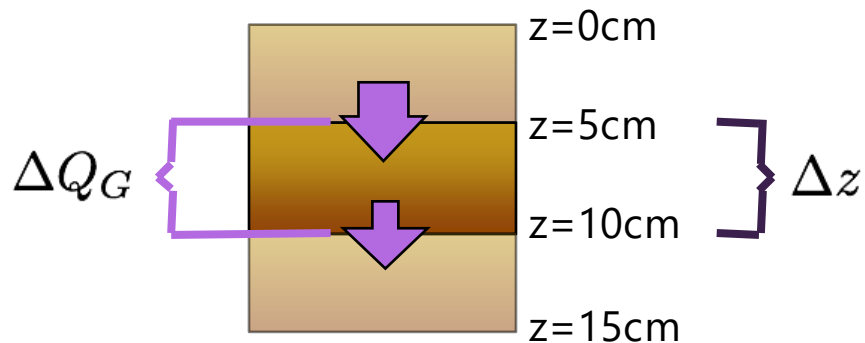
Heat capacity  
in  $\text{J m}^{-3} \text{K}^{-1}$

Heat flux divergence with  
depth  
in  $\text{W m}^{-2} \text{m}^{-1} = \text{W m}^{-3}$

Temperature change  
with time  
in  $\text{K s}^{-1}$

## Warming / cooling of a soil

Re-arranging and writing in finite form gives the **rate of temperature change** in an actual layer of thickness  $\Delta z$  as:



$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

Change of temperature over time in layer (i.e. warming or cooling rate) in  $\text{K s}^{-1}$

Change of heat flux (i.e. input - output) in  $\text{W m}^{-2} \text{m}^{-1}$

★

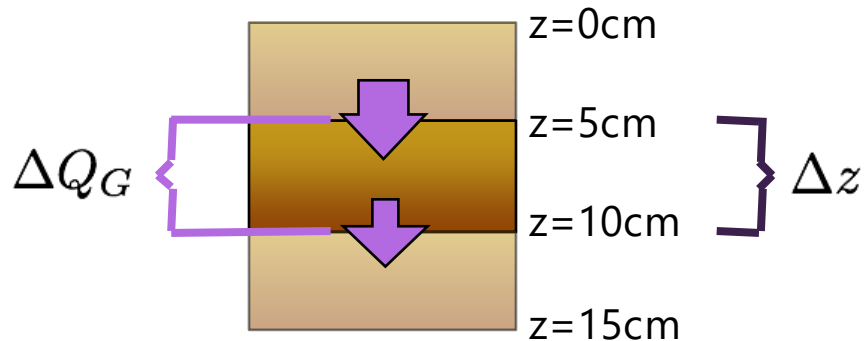




**If the soil has a high heat capacity, the rate of warming or cooling will be:**

A) Higher

B) Lower



Change of heat flux  
(i.e. input - output)  
in  $\text{W m}^{-2} \text{m}^{-1}$

$$\frac{\Delta T}{\Delta t} = \frac{1}{C_s} \frac{\Delta Q_G}{\Delta z}$$

Change of  
temperature over time  
in layer (i.e. warming  
or cooling rate) in  $\text{K s}^{-1}$

★

# Fourier's law

Fourier's law describes that the **flux density of heat conducted**  $Q_G$  is proportional to the **temperature gradient**:

Soil heat flux  
at a given  
depth  
in  $\text{W m}^{-2}$

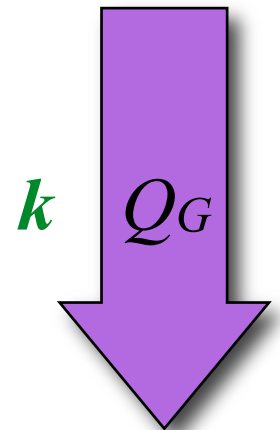
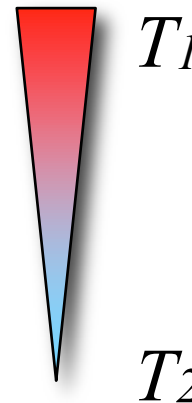
$Q_G$

Temperature  
gradient with depth  
in  $\text{K m}^{-1}$

$$= -k \frac{\partial T}{\partial z}$$

Constant of  
proportionality  $k$  is the  
thermal conductivity (a  
property of the material)  
in  $\text{W m}^{-1} \text{K}^{-1}$

★ (Eq 2)





## Thermal conductivity $k$ of various materials

---

Material	$k$ (W m <sup>-1</sup> K <sup>-1</sup> )
Air	0.025
Water (liquid)	0.59
Ice	2.1
Quartz	8.8
Clay minerals	2.9
Organic matter	0.25
Stainless steel	21
Copper	380

Mineral matter is a good conductor

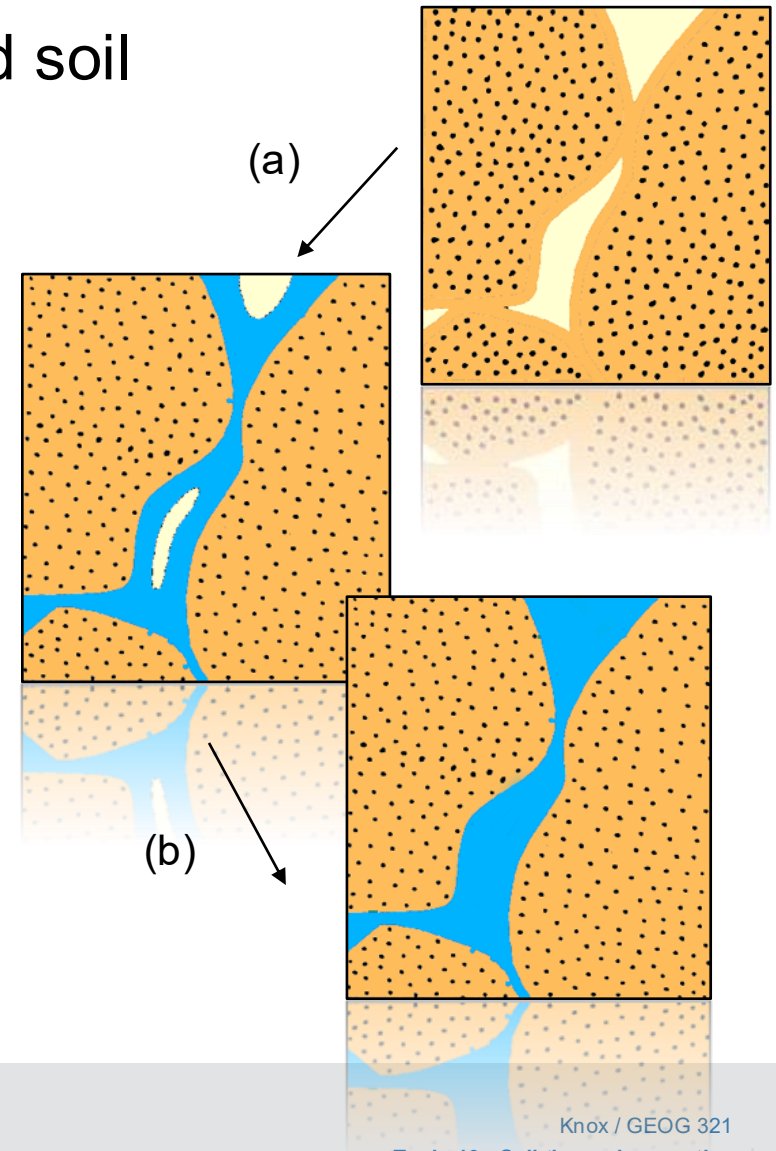
Water is intermediate

Air is very poor

# Thermal conductivity $k$ and water content

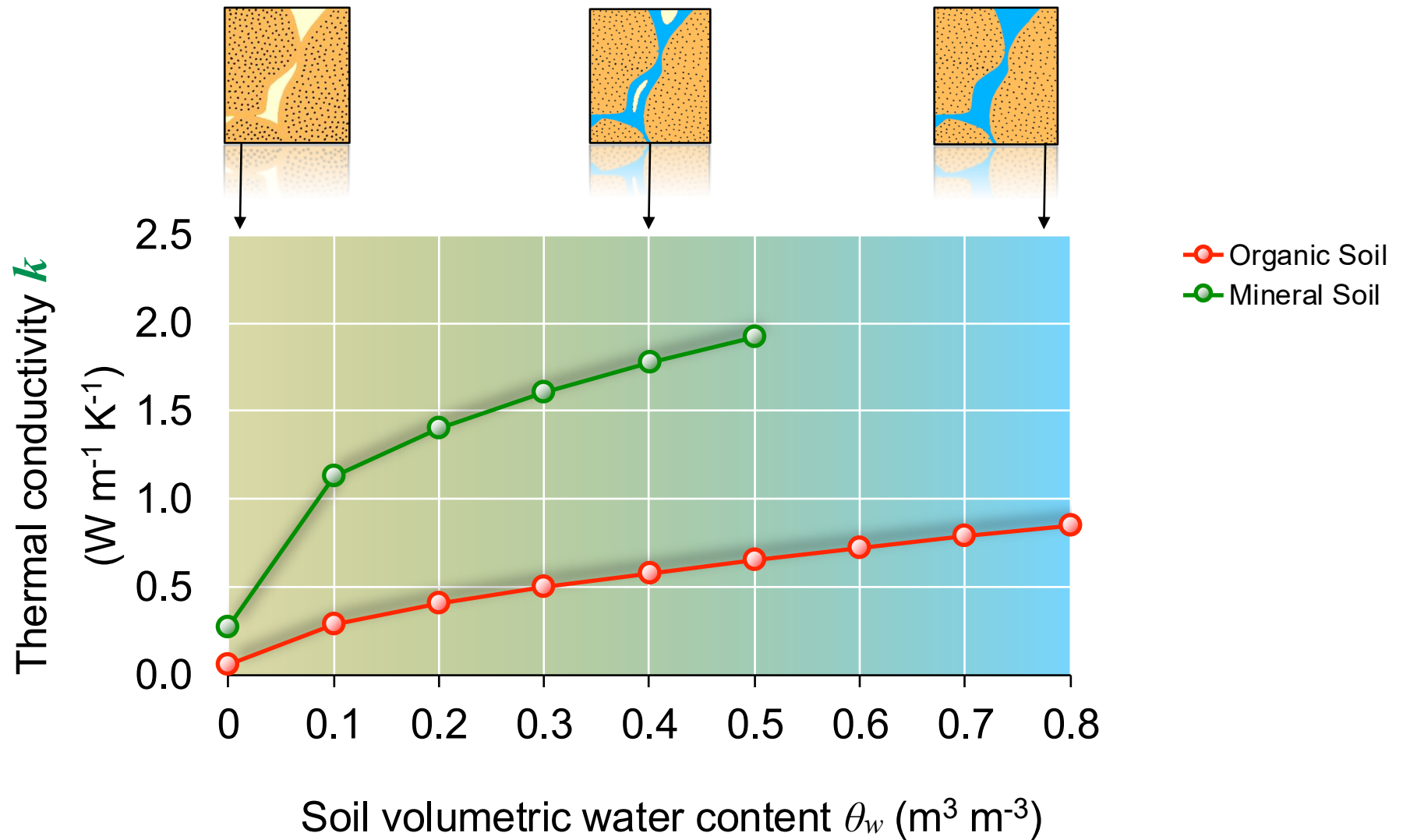
A non-linear relation exists between  $k$  and soil water content ( $\theta_w$ )

- Adding water to dry soil (a) initially causes  $k$  to increase rapidly – rapid increase in area of contacts between soil particles resulting from water film.
- As more water (b) is added,  $k$  increases less rapidly – area of contacts increases more slowly per unit of water added (i.e. diminishing returns).



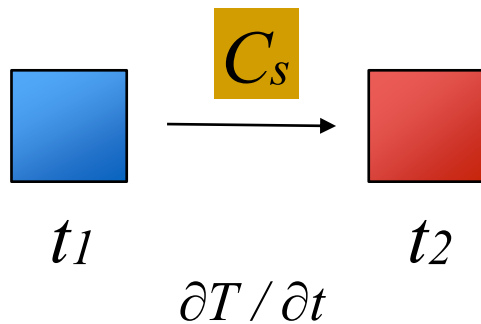


## Soil water content and thermal conductivity $k$

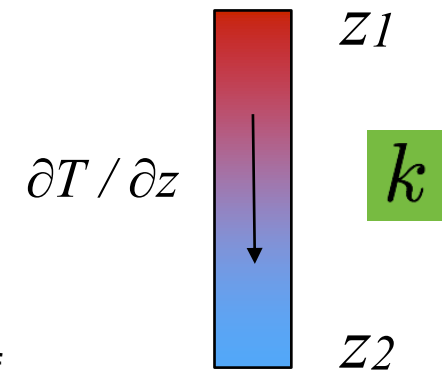


# Combining thermal properties

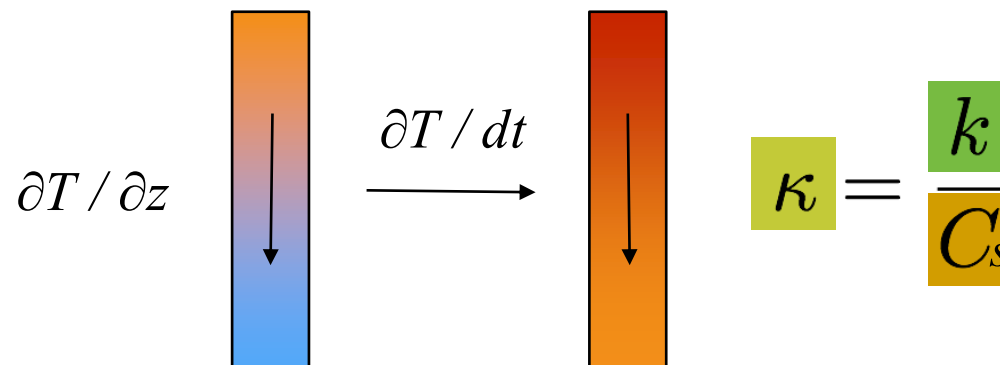
How rapidly does a volume warm when a certain amount of energy is supplied?



How well does heat conduct from one depth to another for a given temperature gradient?



How rapidly does a soil warm at depth if energy is available at the surface?





# Thermal diffusivity

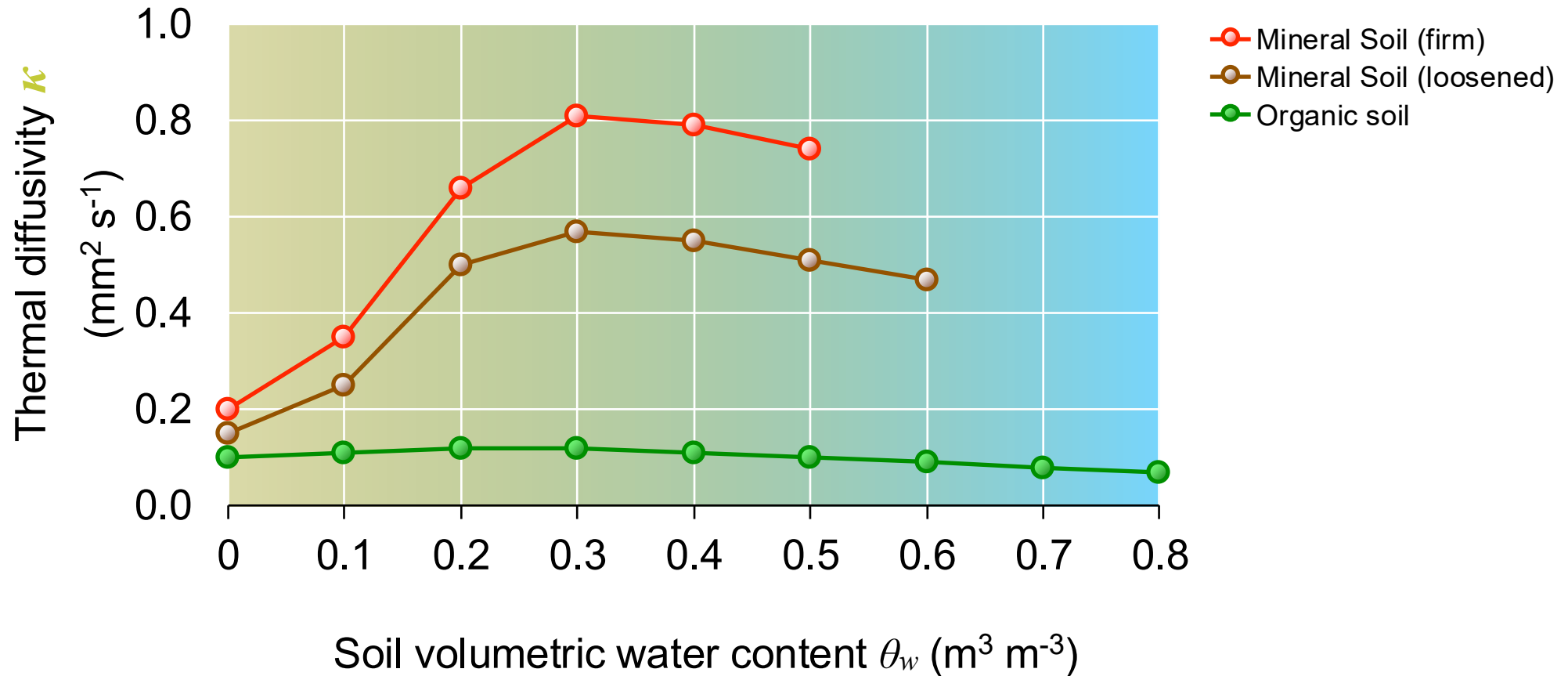
---

**Thermal diffusivity**  $\kappa$  (greek 'kappa' - not 'K') – indicates how quickly soil at depth will warm or cool in response to heating or cooling at the surface. It tells us how fast a temperature wave will diffuse or travel downward into a soil. It is defined:

$$\kappa = \frac{k}{C} \quad \star$$

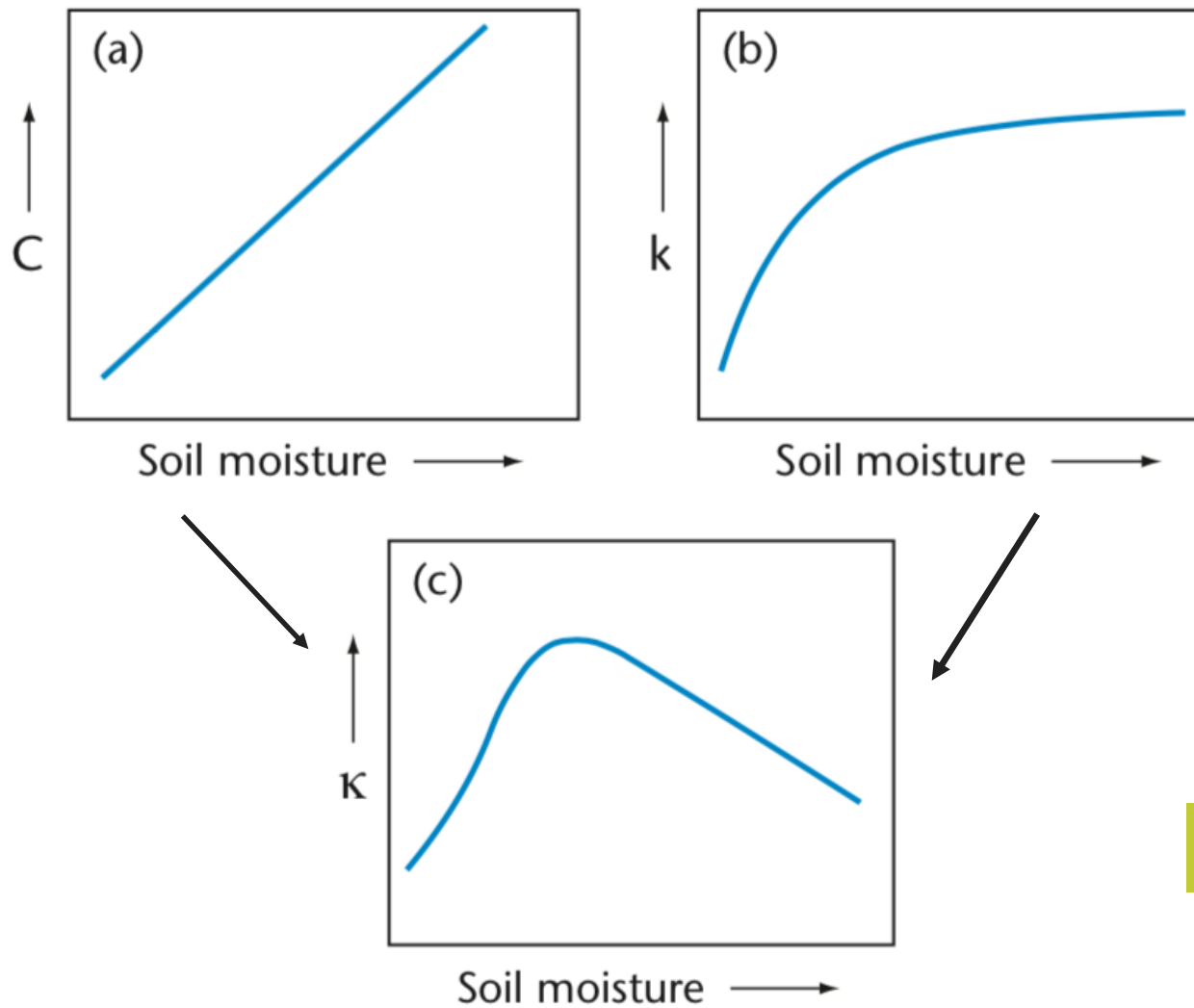
Units:  $\text{m}^2 \text{s}^{-1}$

# Soil water content and thermal diffusivity



Why the curious shape?

## Why the curious shape?



$$\kappa = \frac{k}{C} \quad \star$$



## Take home points

---

- Soils are important for **storage of heat and water** in the climate system.
- Two basic thermal properties regulate the exchange - **Heat capacity**  $C_s$  and **thermal conductivity**  $k$ . From those we can derive **thermal diffusivity**  $\kappa = k / C_s$ .
- The **water content** of the soil is significantly altering both  $C$  (linearly) and  $k$  (non-linearly).